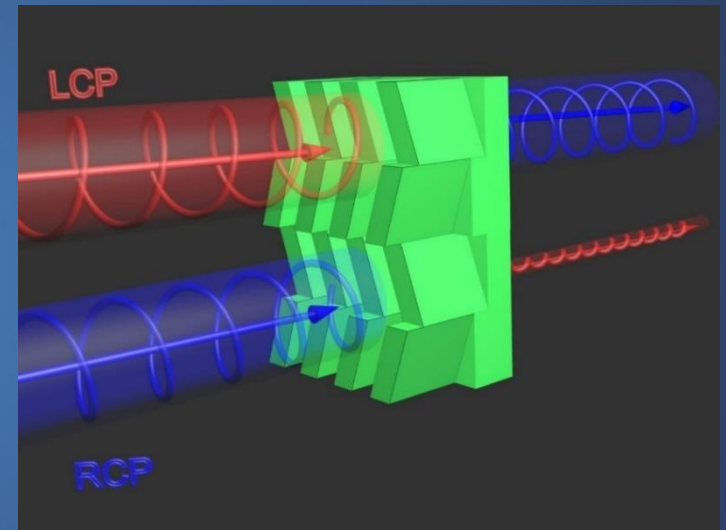


High-Efficiency Asymmetric Transmission of Circularly Polarized THz waves using a Dielectric Herringbone Metasurface

Dr. Mitchell Guy Kenney, S. Li,
X. Zhang, X. Su, T.-T. Kim, D. Wang,
D. Wu, C. Ouyang, J. Han, W. Zhang,
H.-B. Sun, and **Prof. Shuang Zhang**

mitchgkenney@gmail.com
Mitchell.Kenney@Glasgow.ac.uk



M. Kenney *et al.*, Adv. Mater.
28, 9567 (2016)





Overview

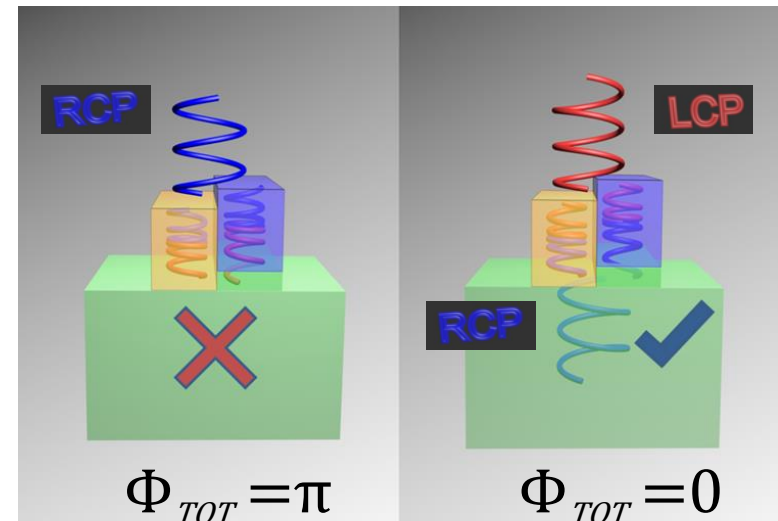


- Primary Objective
- Motivation & Background
- Design
- Simulation & Analytical results
- Fabrication
- Experimental Results
- Conclusion and Future Prospects

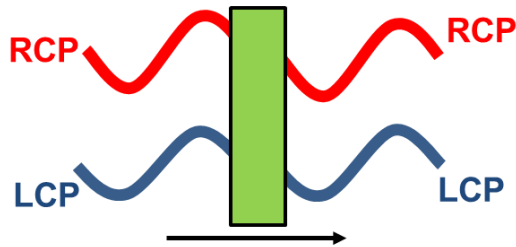
Primary Objective

- Achieve ***Asymmetric Transmission*** (or ***Conversion Circular Dichroism***) in THz regime using **dielectric metasurface**.
- Based on combination of ***Geometric phase*** (Pancharatnam-Berry Phase) and ***Dynamic phase***.

→ Interference between the two phase mechanisms.

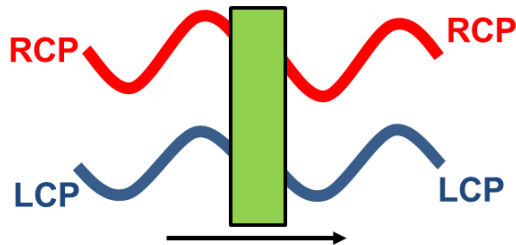


What is Asymmetric Transmission/ Conversion Circular Dichroism?

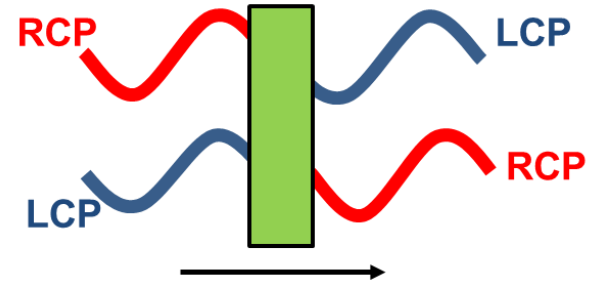


Normal, isotropic homogenous media
Negligible cross-conversion

What is Asymmetric Transmission/ Conversion Circular Dichroism?

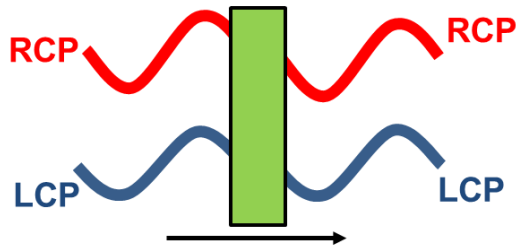


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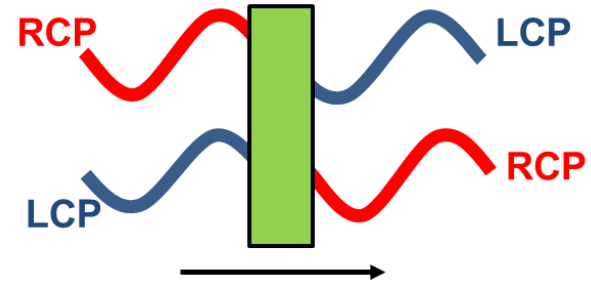


Birefringent media, e.g. half-wave plate
Complete polarisation conversion, large amount
of cross-conversion in equal amounts

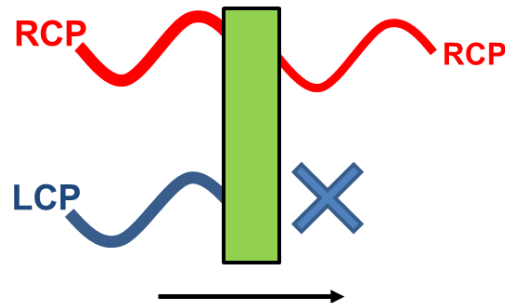
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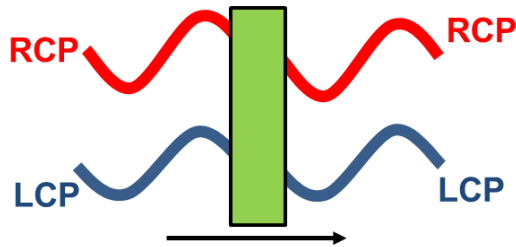


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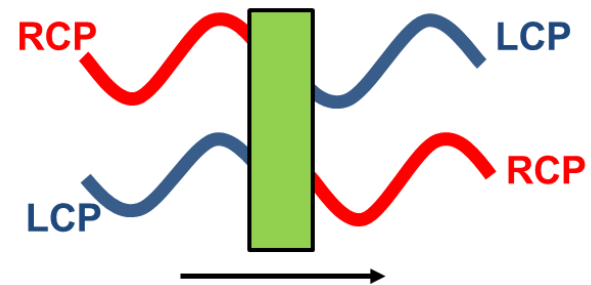


3D chiral media, e.g. helix/spiral
Circular Dichroism, one handedness absorbed more than the other, some cross-conversion

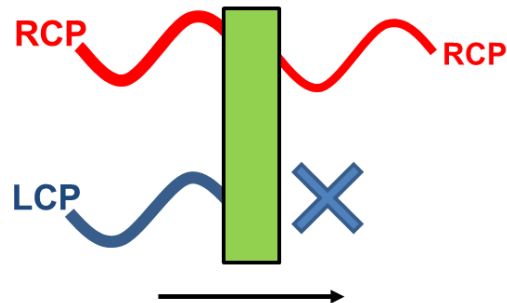
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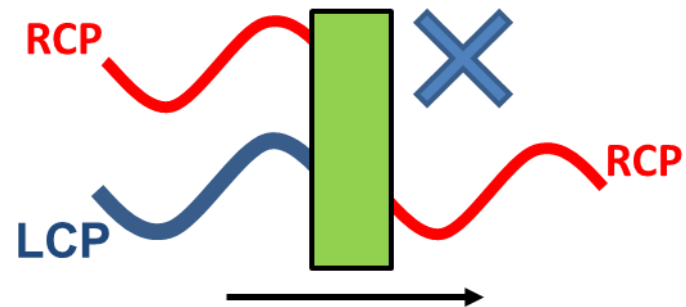
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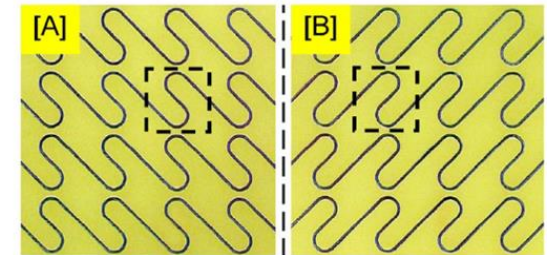
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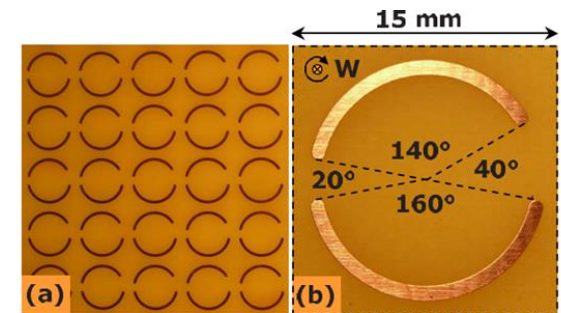
2D chiral media, e.g. meander/asymmetric split ring
Conversion Circular Dichroism (asymmetric transmission), fully flips one handedness, prevents the other (reflection)

Motivation & Background

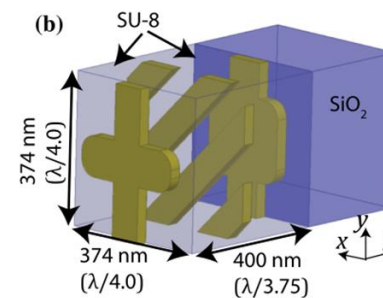
- Previous designs use metal structures \rightarrow lossy!
- For single layer designs, small conversion efficiency
 \rightarrow intrinsic mechanism only allows less than 25% conversion.
- Multilayer designs have better efficiency (53%), but still lossy (37% loss) and involve complex designs/fabrication [Pfeiffer *et al.*]
- Need to develop a 'trivial' method of achieving this phenomenon...



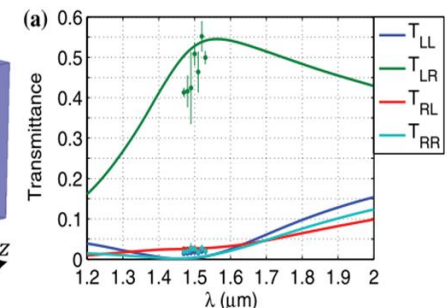
Fedotov *et al.*, *Phys. Rev. Lett.* **97**, 2940 (2006)



Plum *et al.*, *App. Phys. Lett.* **94**, 131901 (2009)



Pfeiffer *et al.*, *Phys. Rev. Lett.* **113**, 023902 (2014)





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Design



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Step 1: Flip the handedness!

Half wave-plate → using Subwavelength Gratings (SWG's)



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Design



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of Glasgow

Step 1: Flip the handedness!

Half wave-plate → using Subwavelength Gratings (SWG's)

Step 2: Introduce phase disparity between handedness' → Geometric Phase

→ Pancharatnam–Berry Phase!

$$\varphi_{Geometric} = \pm 2\theta \text{ ('+' RCP / '-' LCP)}$$

Phase difference between two structures. e.g. $\theta = \pi/4$, so, $\varphi_{Geometric} = \pm \pi/2$.



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Design



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Step 3: Introduce a fixed dynamic phase between the two structures

$\varphi_{Dynamic} = \Delta n_{Si-Air}(2\pi d/\lambda) \rightarrow$ need to get d , the elevation height

$$\varphi_{Dynamic} = +\pi/2$$



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Design



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Total phase is then: $\Phi = \varphi_{Dynamic} \pm \varphi_{Geometric} = \frac{\pi}{2} \pm \frac{\pi}{2} = [0, \pi]$



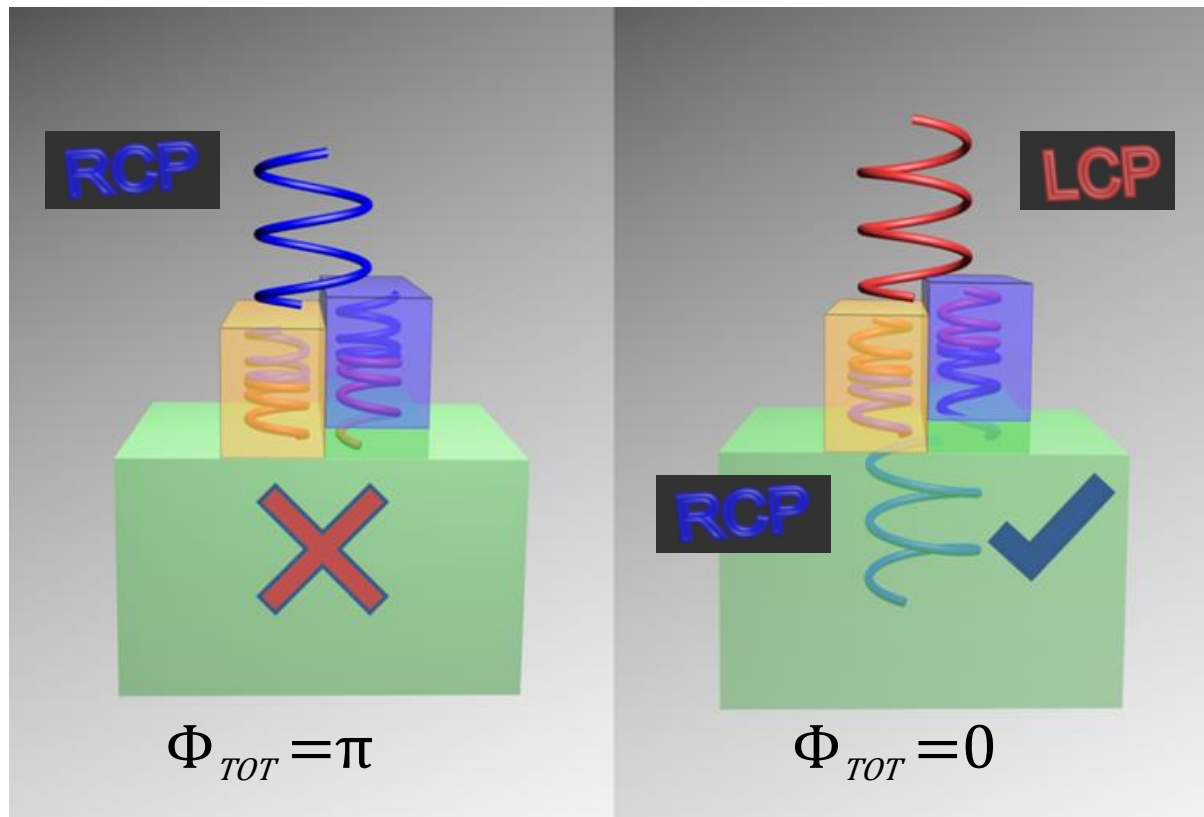
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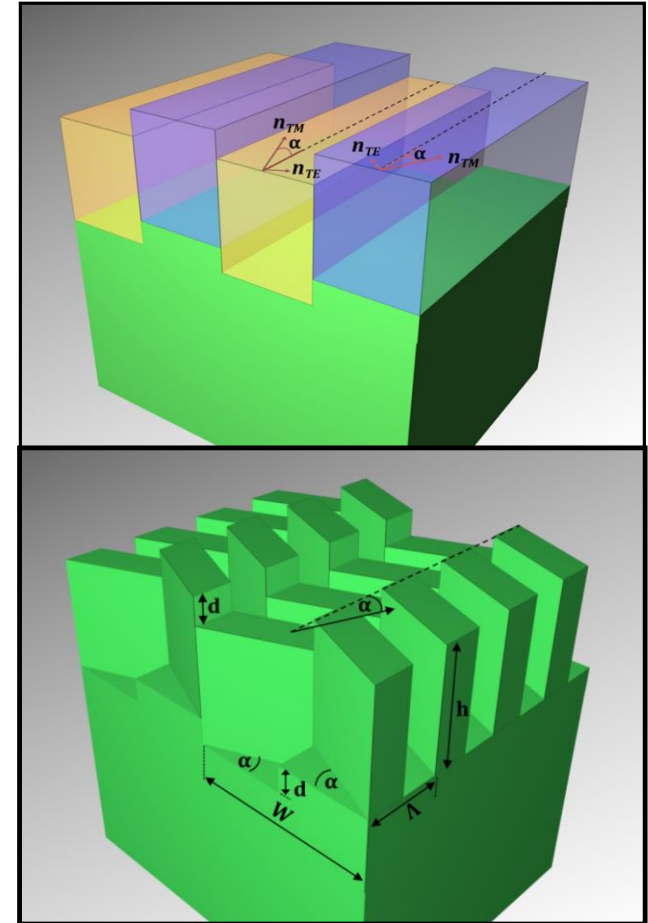
Design

- Designed structure is analogous to using birefringent crystals
- Use Subwavelength gratings for half-wave plate:
→ Period condition is: $\Lambda \leq \lambda/n_{II}$

Λ is period, λ is free-space wavelength, n_{II} is refractive index of substrate

→ Want to perform at 1 THz, use silicon (10kΩ):
 $\lambda = 300 \mu\text{m}$, $n_{II} = 3.418 \rightarrow \Lambda \leq 87.7 \mu\text{m}$

Choose $\Lambda = 86 \mu\text{m}$



- Need to calculate depth and duty-cycle of SWG's.

Grating equation:

$$\Delta\Phi_{TE-TM}(\lambda) = \left(\frac{2\pi h}{\lambda}\right) \Delta n_{form}(\lambda)$$

- $\Delta\Phi_{TE-TM}$ is the (wavelength-dependent) phase difference between parallel (TE) and perpendicular (TM) components of light in the grating
- h is the depth of the gratings
- Δn_{form} is the difference in refractive indices along the TE and TM directions of the grating, given as:

$$\Delta n_{form} = n_{TE}(\lambda) - n_{TM}(\lambda)$$

$$n_{TE} = (Fn_I^2 + (1-F)n_{II}^2)^{1/2}$$

$$n_{TM} = (Fn_I^{-2} + (1-F)n_{II}^{-2})^{-1/2}$$

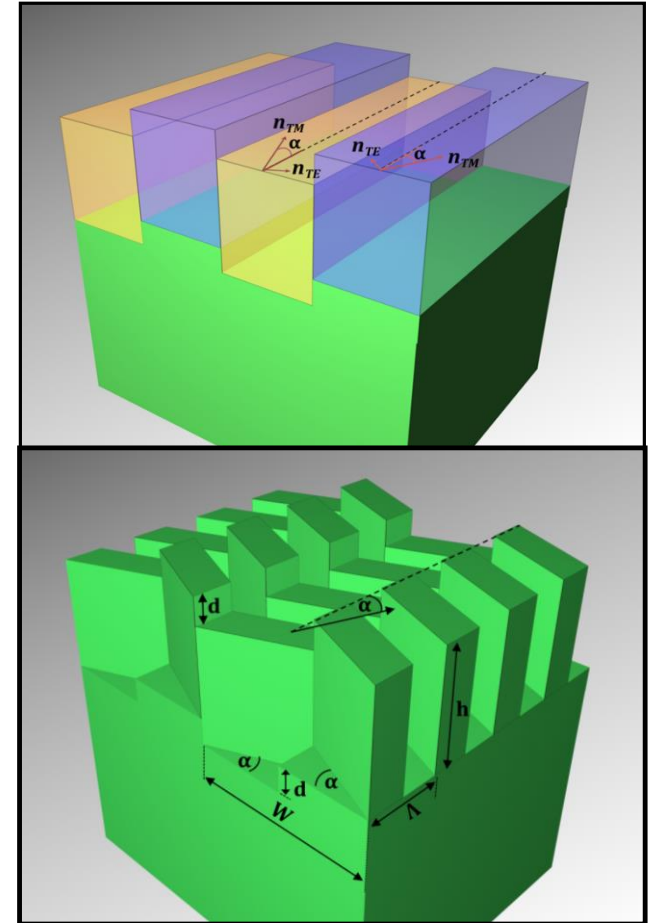
- Using a duty cycle of $F = 0.5$, and $n_I = 1$ for air, we have:

$$n_{TE} = 2.52$$

$$n_{TM} = 1.36$$



$$\Delta n_{form}(\lambda) = 1.16$$



Design

$$\Delta n_{form}(\lambda) = 1.16 \rightarrow \Delta \Phi_{TE-TM}(\lambda) = \left(\frac{2\pi h}{\lambda} \right) \Delta n_{form}(\lambda)$$

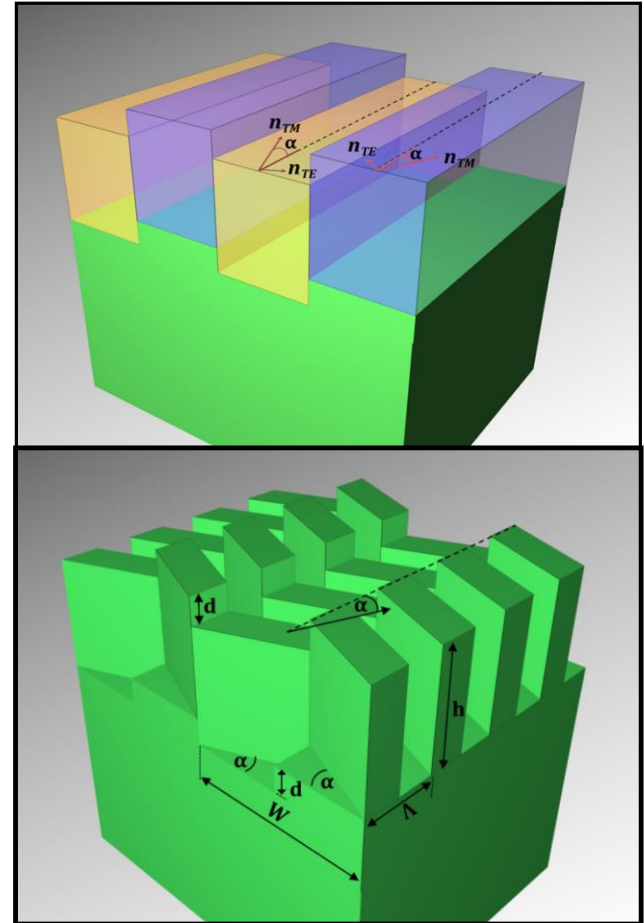
- Want Half-wave plate functionality, choose $\Delta \Phi = \pi$

Rearrange to get $h = 129 \mu\text{m}$

- Apply P-B phase of $\pi/2$ by setting $\alpha = 22.5^\circ$
- Apply dynamic phase of $\pi/2$ by adding a step beneath one grating, need to calculate step height d

Use equation: $\Delta \varphi_{Dyn} = \Delta n_{Si-Air}(2\pi d/\lambda)$

Simply get $d = 31 \mu\text{m}$





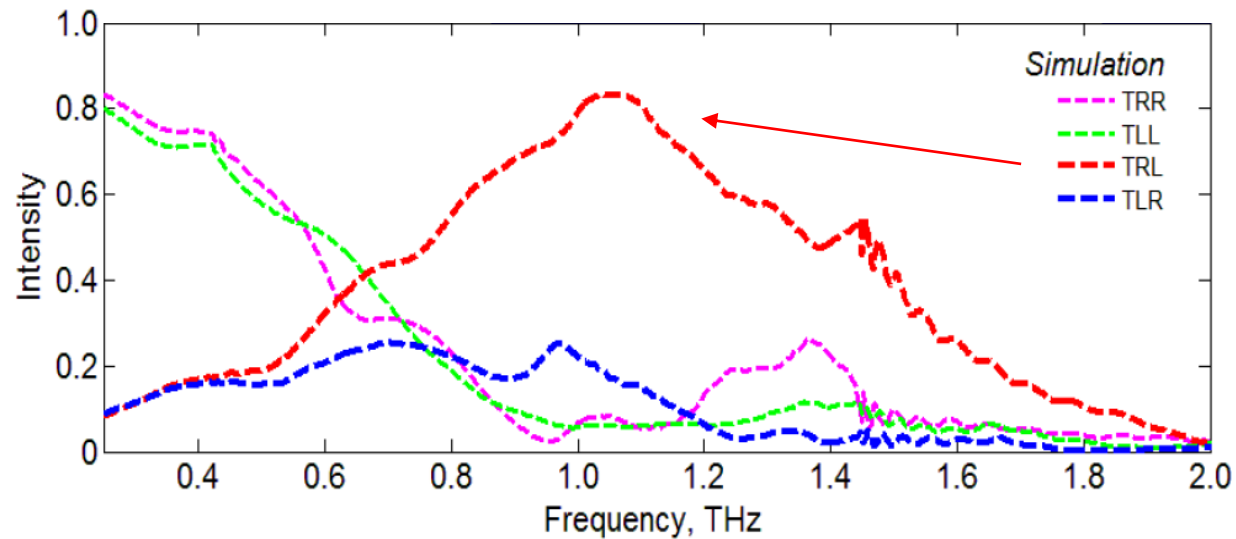
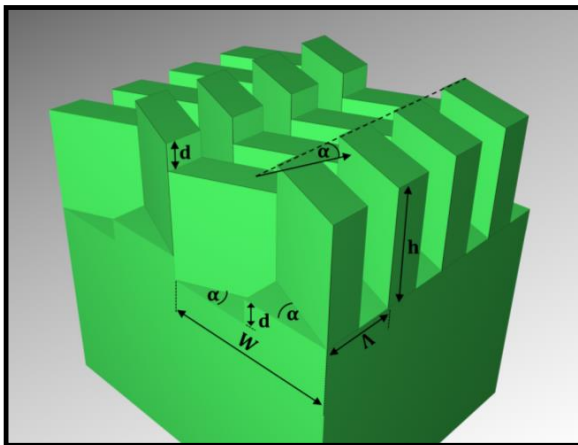
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Simulation



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- Simulate using CST Microwave studio



- Very high cross polarisation, $T_{RL} \approx 85\%$ @ 1.05THz
- T_{LR} is low (15% @ 1.05THz) as required
- Unconverted (co-pol.) values are low, $<10\%$ @ 1.05THz



Analytical



- Use analytical model based on Fresnel's equations for a three-layer system.

$$t_i = \frac{t_{12i} t_{23i} e^{-i\phi}}{1 + r_{12i} r_{23i} e^{-2i\phi}}$$

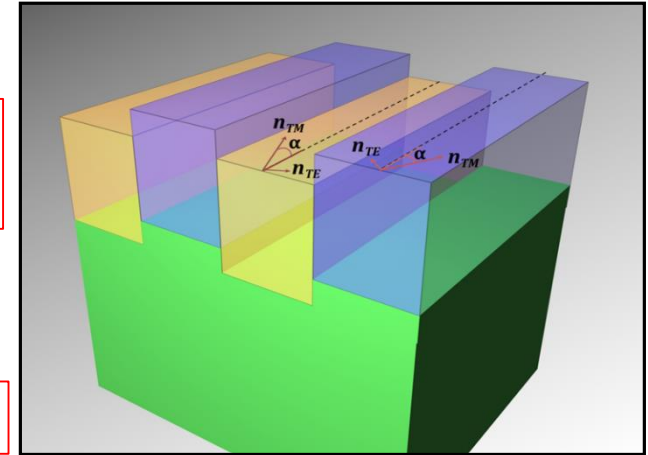
$$\phi_i = \frac{2\pi d}{\lambda} n_{2i}$$

$$t_{12i} = 2n_1 / (n_1 + n_{2i})$$

$$t_{23i} = 2n_{2i} / (n_{2i} + n_3)$$

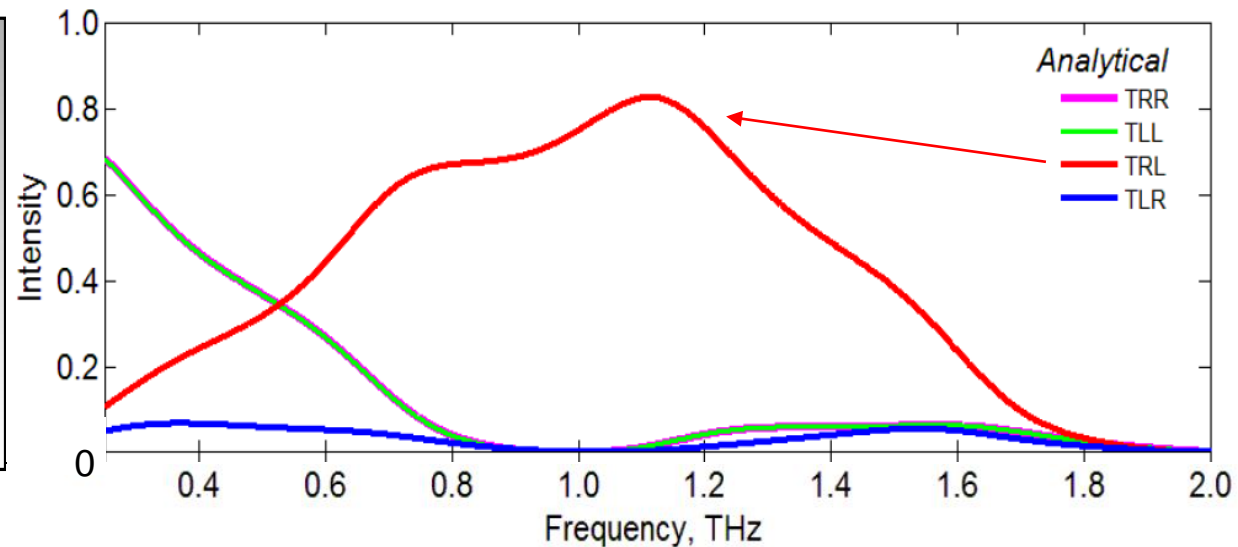
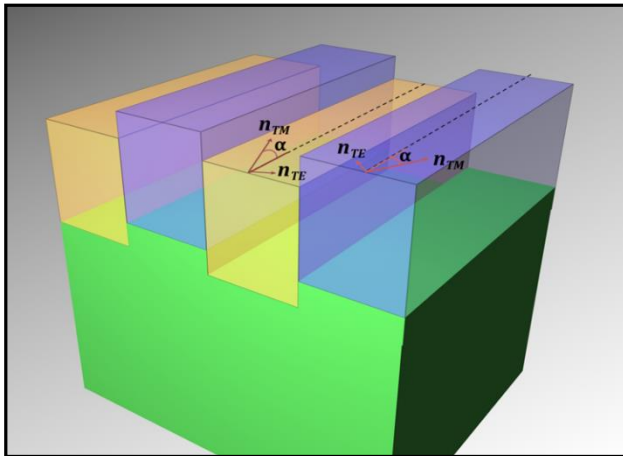
$$r_{12i} = (n_1 - n_{2i}) / (n_1 + n_{2i})$$

$$r_{23i} = (n_{2i} - n_3) / (n_{2i} + n_3)$$

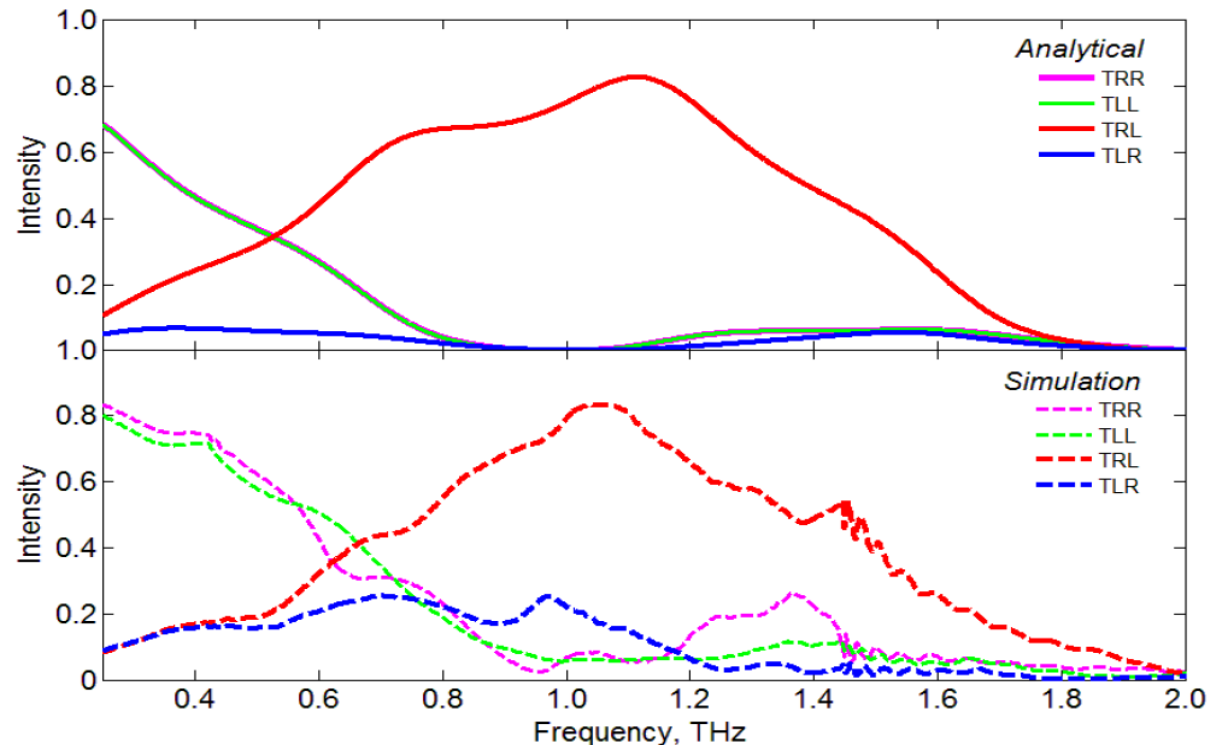
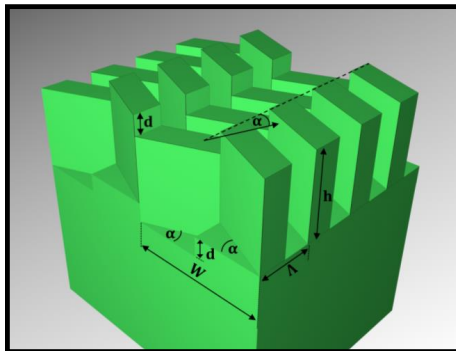
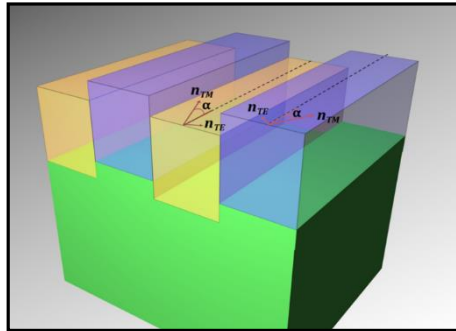


- Use this equation to describe yellow SWG without phases
- Introduce P-B and dynamic phases to 2nd blue SWG, sum the two transmittances together:

$$T = n_3 \left| \frac{1}{2} (t + t \cdot e^{i\phi_{Dyn}} \cdot e^{i\phi_{Geom}}) \right|^2$$



- Similar results to simulation
- Very high cross polarisation, $T_{RL} \approx 85\%$ @ 1.1THz
- T_{LR} is low ($\sim 1\%$ @ 1.1THz)
- Unconverted (co-pol.) values are low, $< 1\%$ @ 1.1THz



- Slight mismatch in central frequency and design of 1 THz
 - SWG's are based on 1st order effective medium theory, period actually $\sim 80\mu\text{m}$
 - Fabry- Pérot effects between layers, differs from single-pass theory
 - SWG's & step not dispersionless, operation changes for wavelength



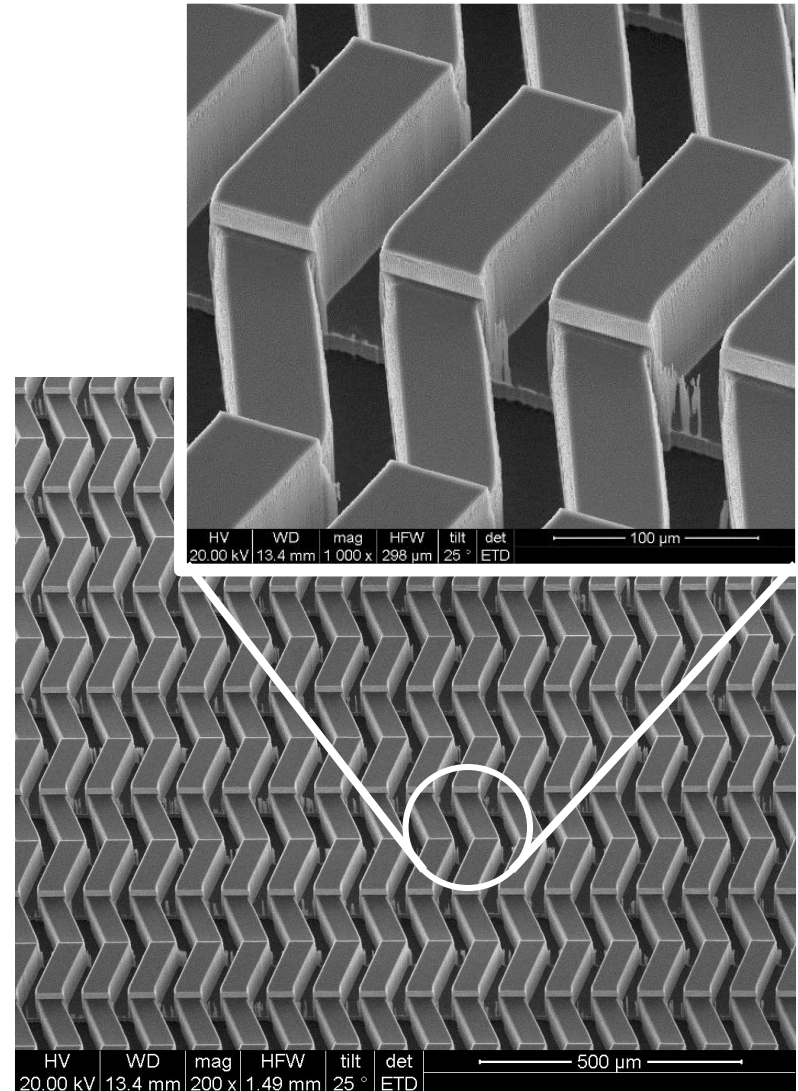
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Fabrication



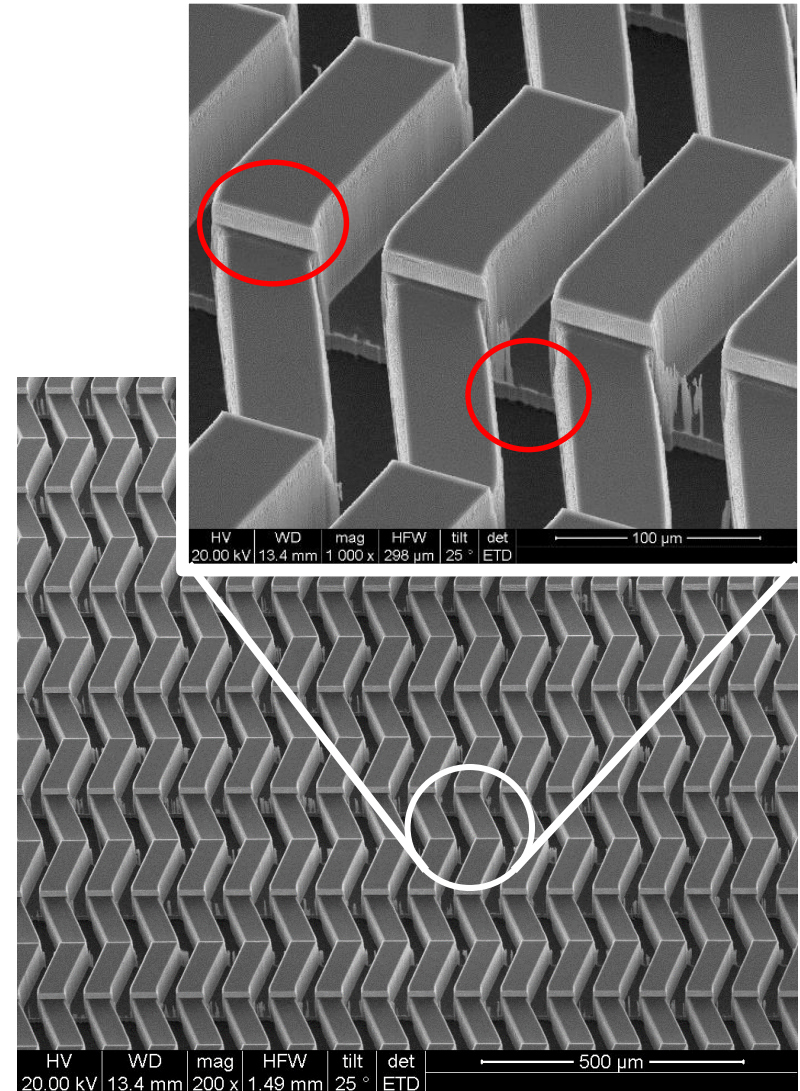
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- Standard photolithography and Deep Reactive Ion Etching used to fabricate silicon wafer
- First, stripes of $31\text{ }\mu\text{m}$ step are fabricated by etching
- Then, zig-zags overlaid, and etched down $129\text{ }\mu\text{m}$.



Fabrication

- Standard photolithography and Deep Reactive Ion Etching used to fabricate silicon wafer
- First, stripes of $31\text{ }\mu\text{m}$ step are fabricated by etching
- Then, zig-zags overlaid, and etched down $129\text{ }\mu\text{m}$.
- Slight difference between bottom step and top step (red circles)
→ Re-simulate to reflect this





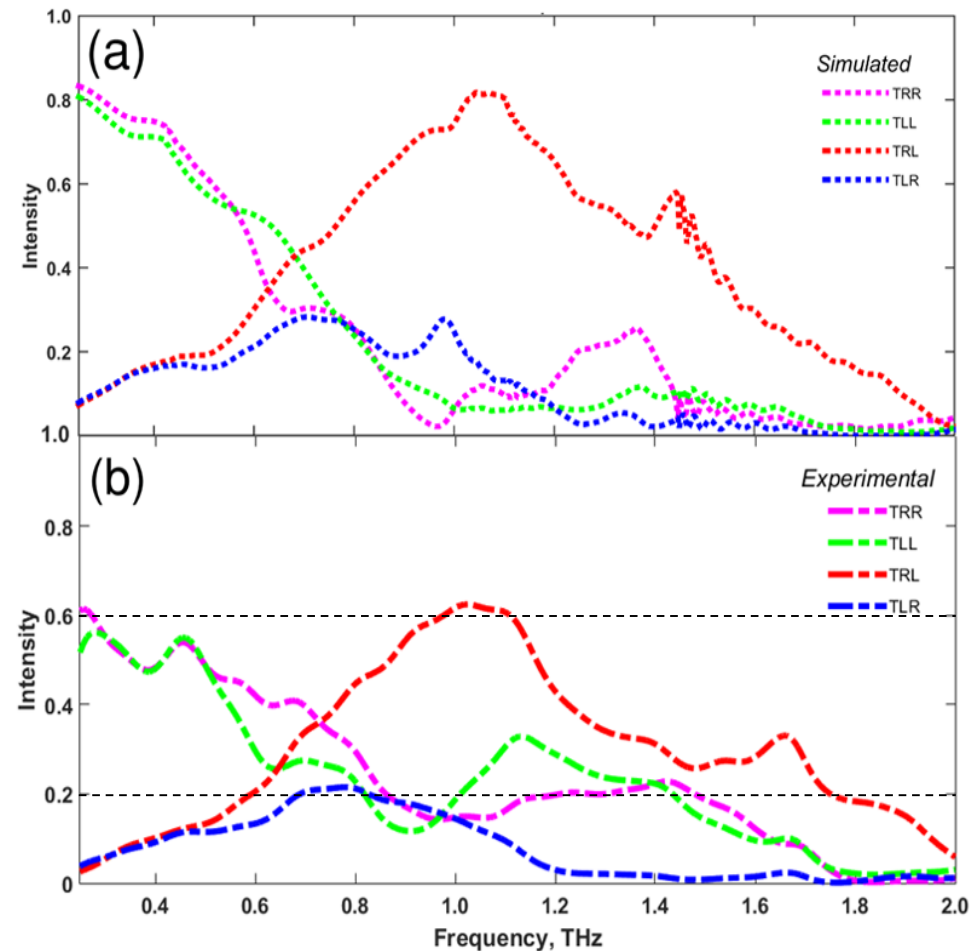
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Experimental Results



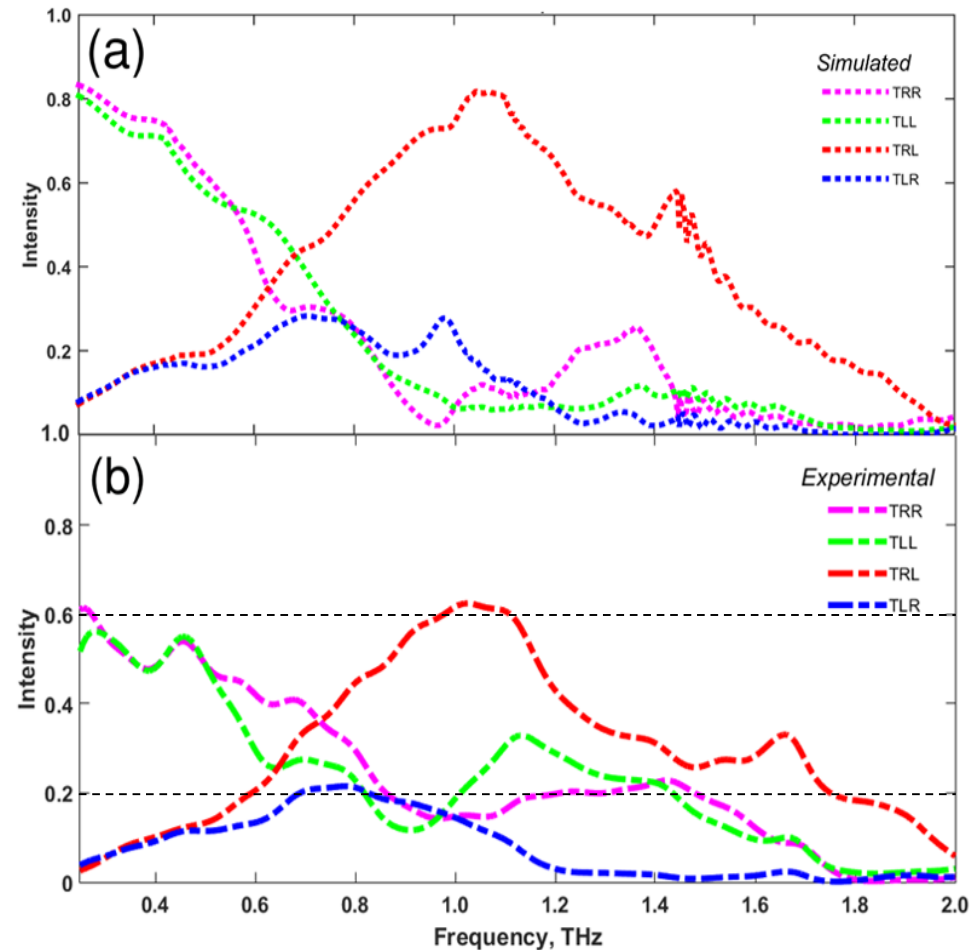
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- Simulation not too different to previous 'desired' parameters
- THz-TDS (Time Domain Spectroscopy) used to obtain experimental data.
→ Linear polarisation, post-processing to convert to circular basis
- Experimental result impressive
→ $T_{RL} \approx 63\%$ @ 1.025THz
→ $T_{LR} \approx 13\%$
→ Extinction ratio approx. 5:1
- Un-converted polarisations are <20%
- Difference between exp. & sim. due to fabrication errors, step mismatch, and side-wall slope, material losses



Experimental Results

- Very broadband, FWHM of 0.72 THz at central frequency of 1.025 THz $\rightarrow \Delta f/f = 70\%$
- Total energy, T_R and T_L :
 $\rightarrow T_R = 28\%$
 $\rightarrow T_L = 84\%$
- $R = 1 - T$ (ignore absorption)
 \rightarrow Implies that R_R is 72%
- The device can be used to distinguish between L and R to a high efficiency



Conclusion

- Achieved Asymmetric Transmission/Conversion Circular Dichroism using dielectric metasurface, not metallic
- Straight-forward approach, rather than trial-and-error optimization of impedances between layers etc...
- Obtained highest recorded AT of 63% (to our knowledge) in the THz regime (possibly all regimes)
- Very broadband, $\Delta f/f = 70\%$, and extinction ratio of 5:1 between T_{RL} and T_{LR}
- $TL = 84\%$ and $RR = 72\%$, can use device to distinguish handedness of incident light to high efficiency

Future Prospects

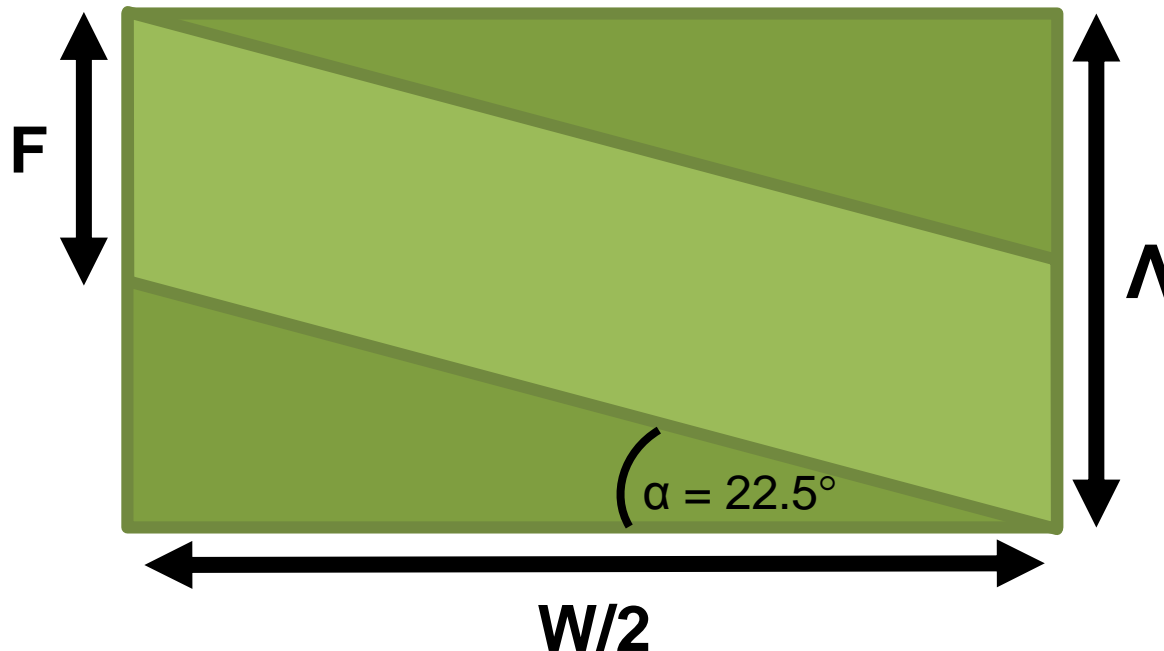
- Potential for use in other frequency regimes
- Dielectric nanobricks, e.g. TiO_2 for visible light, act as half-wave plates
 - incorporate extra phase step beneath opposing element to induce handedness dependence
- Could have holograms which only operate for one handedness, have holographic image in different quadrants in +Z and -Z axis
- Linear-to-circular lenses, using P-B phase with only one foci, not two



Thank you

Subwavelength Gratings

- Duty cycle, $F = 0.5$
- $\Lambda = 86 \mu\text{m}$, not quite equal to actual period of gratings
→ actual period $\sim 80 \mu\text{m}$
- $W = 208 \mu\text{m}$, due to geometry



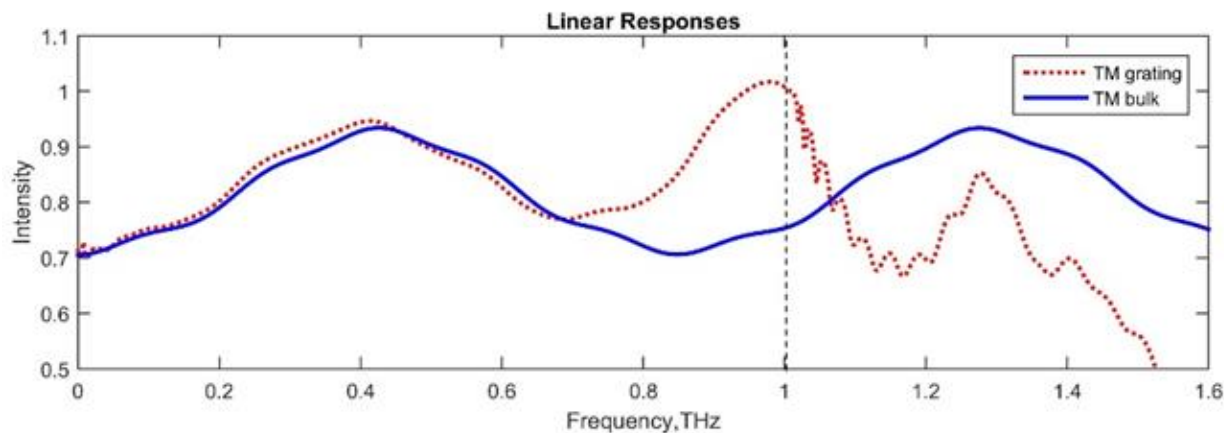
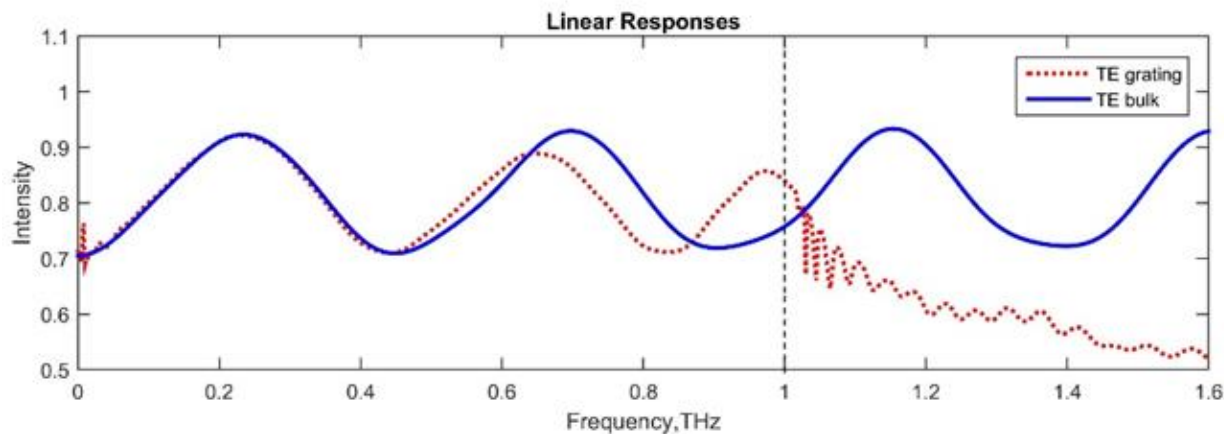


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Subwavelength Gratings



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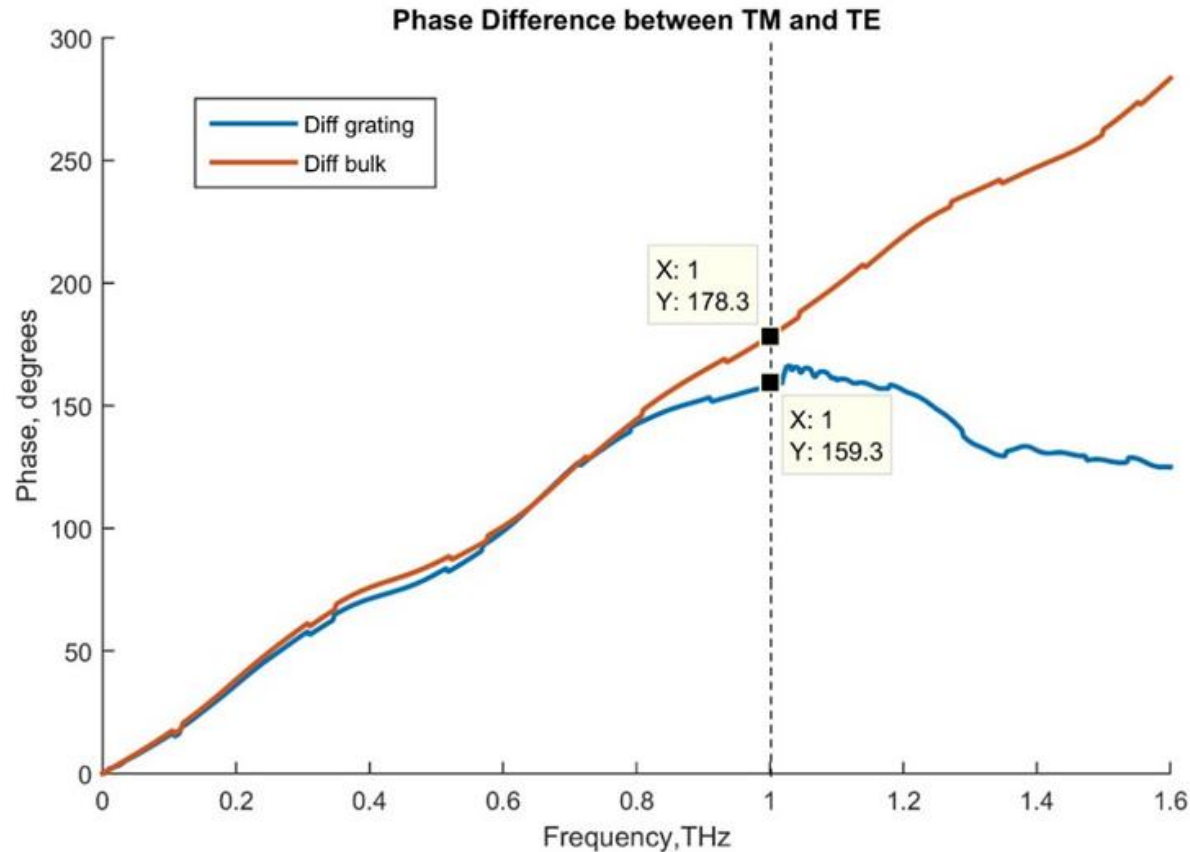
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Subwavelength Gratings



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- Grating not too different to 'desired' bulk parameters
→ approx. π phase difference → Half-wave plate





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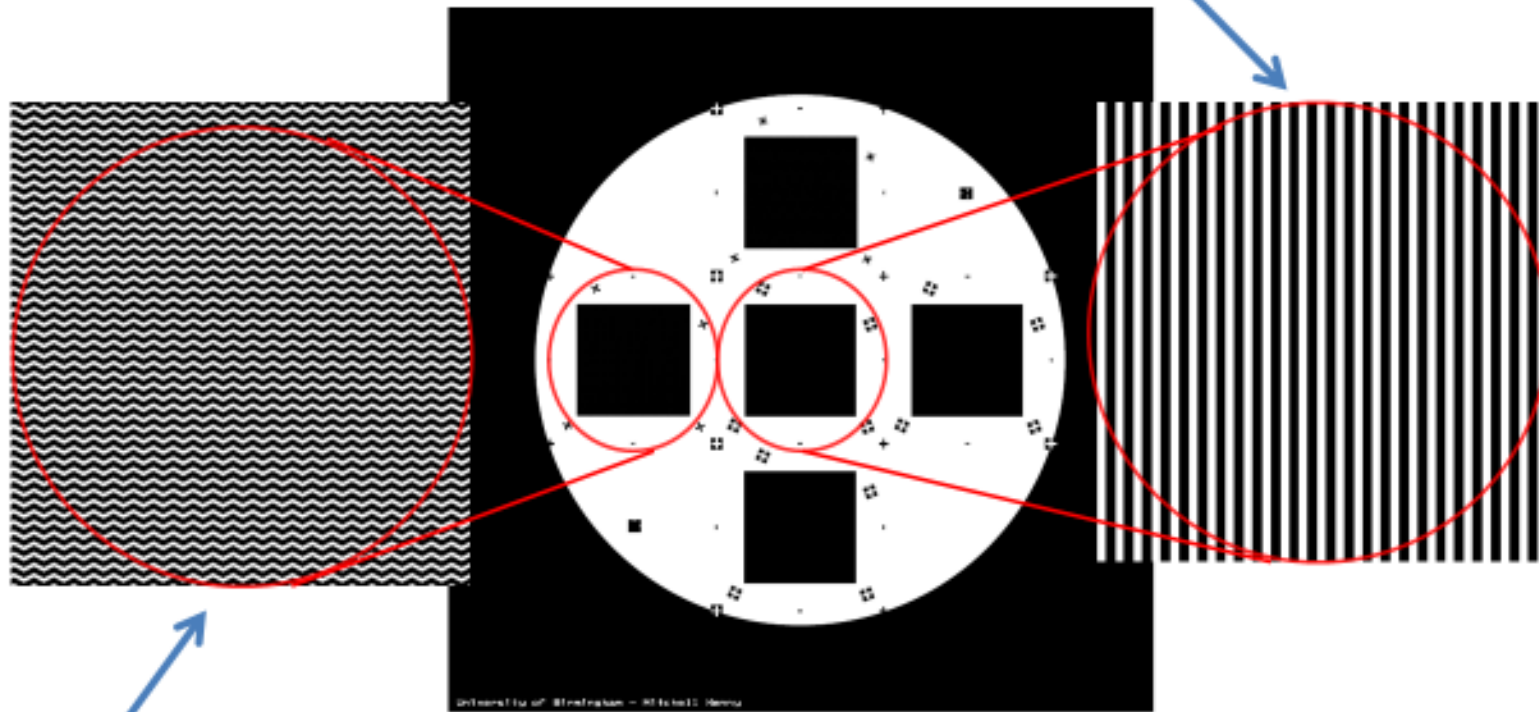
Fabrication



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Photomask

1st Pattern to etch - STRIPES



2nd Pattern to etch - ZIGZAGS



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Fabrication



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Procedure

